

NRL Memorandum Report 5384

# An Automated Immittance Measuring System for Electroacoustic Transducers

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Underwater Sound Reference Detachment P.O. Box 8337 Orlando, Florida 32856

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Analyzer. The algorithm determines the frequencies at maximum and minimum immittances,						
the series and parallel resonance frequencies, and the resonance and antiresonance						
frequencies as well as the mechanical quality factor of the element under test. The						
collected data are plotted in the form of either admittance or impedance loops with evenly						
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#### INTRODUCTION

The precise measurement of immittance is a valuable tool for the analysis of electroacoustic transducers and piezoelectric materials. Immittance is used in the determination of transducer efficiency, electrical matching, and the tuning and analysis of transducer performance and of material parameters of active transducer materials. Previous techniques for immittance measurements involved the use of such devices as impedance bridges, analog voltmeters, phase meters, and some special analog devices like the vector impedance meter. All of the before mentioned devices suffer from one or more restrictions; e.g., speed, precision, or stability.

The HP Model 4192A Digital Network Analyzer is computer controlled and has the ability to make immittance measurements at high speed with excellent precision and stability. Combined with the developed circular approximation algorithm, the measurements can be made with greater efficiency to provide the maximum amount of information with the minimum number of data points. This method also allows for fast, accurate computation of critical points of immittance without knowing the series (parallel) resonance of the transducer. The optimization of data points is achieved by the determination of frequencies that will be quasi-uniformly distributed around the immittance circle as opposed to the "clustering" of frequencies above and below the frequency of maximum immittance.

Figure 1 compares an immittance circle defined by a linear sequence of frequencies with one in which the frequencies are generated from the circular approximation method. There are two hundred points in the linear frequency sweep of Fig. 1a and only fifty points in Fig. 1b. This circular approximation method has been implemented on various piezoelectric transducers and works exceptionally well in most cases. The timesaving is greatest when measuring high-Q transducers. Linear-spaced frequency points appear diluted on the steep slopes of the imaginary part of a high-Q immittance, as shown in Fig. 2. For low-Q curves the frequency distribution is more evenly spaced. When the data are presented in the form of imaginary verses real immittance, the data from high-Q systems are

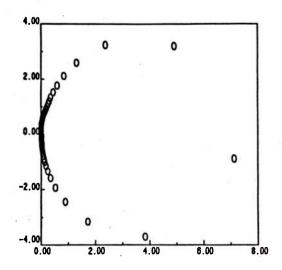


Fig. 1a - Immittance loop showing the distribution of data points resulting from a linear sweep of two hundred frequency steps.

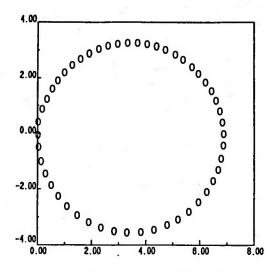


Fig. 1b - Immittance loop showing the more uniform distribution of only 50 data points when frequencies are determined by the circular approximation method.

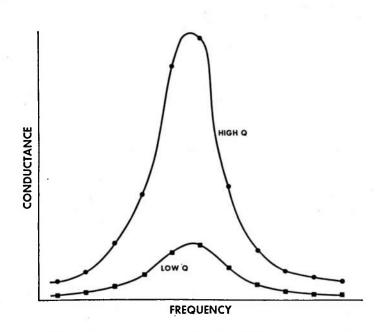


Fig. 2 - Distribution of data points for equally spaced frequencies on the imaginary part of the immittance curve for a high-Q system and for a low-Q system.

concentrated near the beginning and end of the immittance circle. For low-Q systems the data points approach a uniform distribution.

#### CIRCULAR APPROXIMATION ALGORITHM

The circular approximation method can be applied to admittance and impedance loops. Because of the similarity of application to impedance and admittance, and to avoid writing "impedance or admittance", the two quantities are implied when the term immittance is used in the following text. The differences between the admittance terms and the impedance terms will be discussed in the PROGRAM section of this report. Thoughout this report the word "points" appears many times with various meanings. To assure clarity three symbols are defined:

- o The term "points(f)" refers to a frequency.
- o The term "points(c)" refers to the ordered pair on the theoretical circle.
- o The term "points(i)" refers to the real and imaginary position on the immittance loop.

The method presented here will be based on the following equation:

$$\tan(\Theta) = \frac{L\left[\omega^2 - \omega_1^2\right]}{\omega R}.$$
 [1]

This equation is derived [1] from a simple equivalent circuit of a piezoelectric resonator, where L is the inductance,  $\omega$  is the angular frequency,  $\omega_{\bf i}$  is a resonant frequency (series resonance when measuring admittance, parallel resonance when measuring impedance),  $\Theta$  is the phase angle, and R is the resistance. Cady uses  $\omega_{\bf 0}$  (angular frequency of zero crossing) in Eq. (1) instead of  $\omega_{\bf i}$ . But  $\omega_{\bf i}$  is also an angular frequency at a zero crossing since a transformation of axes is performed with the circular approximation method. It is algebraically convenient to write Eq. (1) in the following form: Given  $\omega$ , R, and  $\Theta$  for three points(f),  $\omega_{\bf i}$ 

and L are determined by applying Cramer's rule [2] to this expression:

$$\omega_{i}^{2} + \frac{1}{L} \omega R tan(\Theta) = \omega^{2}.$$
 [2]

By using the following equation

$$L\omega^2 - L\omega_i^2 - \omega R \tan(\Theta) = 0,$$
 [3]

the angular frequencies ( $\omega$ ) are determined as a function of the angle  $\Theta$  by solving the quadratic equation. Equations (2) and (3) are the key equations used in the circle approximation method and will be referred to many times in the text of this paper. The argument used for applying Eqs. (1) through (3) to both impedance and admittance is found in Appendix A.

The algorithm used in determining the admittance or impedance loops consists of two major parts. First, the "best fit" circle that approximates the immittance loop is determined from parameters of the simple equivalent circuit of a piezoelectric resonator. Secondly, the circular approximation is then divided into equal arcs that are used to determine quasi-equally spaced points(i) on the immittance loop.

To determine the "best-fit" circle, one must first identify any three frequency points(f) on the immittance loop with the abscissa and ordinate identified as conductance and susceptance (or resistance and reactance), respectively. If previous knowledge exists about the transducer to be measured, these three points(f) are easy to identify. If however, there is no previous knowledge about the transducer, the program will assist the user in determining the three points(f).

The HP 4192 Impedance Analyzer measures the real and imaginary parts of immittance at each of these frequency points(f) and the ordered pairs of data are stored as  $(x_i, y_i)$ , where i goes from 1 to 3 corresponding to each of the three frequency points(f). These ordered pairs are used in the general form of the equation of a circle:

$$x_i D + y_i E + F = -[x_i^2 + y_i^2]$$
 (4)

of center 
$$\left[\frac{-D}{2}, \frac{-E}{2}\right]$$
 and radius  $\frac{1}{2}\left[D^2 + E^2 - 4F\right]^{1/2}$ . [5]

To find D, E, and F, we impose the condition that the coordinates of each of the given points(i&c) satisfy Eq. (4). When these values for D, E, and F are substituted in Eq. (5), we have the radius and center of the circle through the given points(i&c). By using the calculated radius and center, two points(c) located 120 degrees from a fixed initial point(i&c) are found as shown by the boxes in Fig. 1. The authors have arbitrarily chosen the fixed point(c) to be the second initial point(i). One may use any initial point(i) as long as it remains consistent throughout the entire procedure.

In order that this procedure apply both to loaded and unloaded transducers, a translation of axes is performed on all points(i) used in Eqs. (2) and (3). The formulas for the translation of axes are:

$$x_{+} = x_{0} - x_{C} + r$$
 and  $y_{+} = y_{0} - y_{C}$  [6]

where  $(\mathbf{x}_{\mathbf{C}} + \mathbf{r}, \mathbf{y}_{\mathbf{C}})$  is the new origin. The ordered pair  $(\mathbf{x}_{\mathbf{C}}, \mathbf{y}_{\mathbf{C}})$  is the center of the circle, r is the radius,  $(\mathbf{x}_{\mathbf{O}}, \mathbf{y}_{\mathbf{O}})$  are the old coordinates, and  $(\mathbf{x}_{\mathbf{t}}, \mathbf{y}_{\mathbf{t}})$  are the old coordinates with the new origin. The slope  $[\tan(\theta)]$  is determined by first applying Eqs. (6) to a given point(i). The resistance R, also found in the Eqs. (2) and (3), is replaced by the diameter or reciprocal of the diameter of the circle depending on which immittance loop is chosen. The quantities  $\omega_{\mathbf{i}}$  and L are calculated using Eq. (2) and the data of two intial points(i) along with information from the circle. With the calculated parameters  $(\omega_{\mathbf{i}}, \mathbf{L}, \text{ and } \theta)$  of the two 120-degree points(c), the frequencies  $(\omega/2\pi)$  at the 120-degree points(c) are calculated by applying Eq. (3). The HP 4192 Impedance Analyzer measures the conductance and susceptance (or resistance and reactance) at each frequency, and the points(i) are stored. These points(i) are illustrated by the "triangles" in Fig. 3.

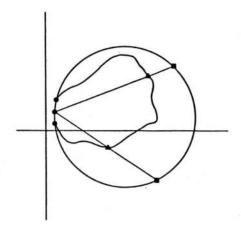


Fig. 3 - An immittance loop with a first-circle approximation.

Dots indicate the first three frequencies chosen.

Squares mark the 120° points.

Triangles represent associated points on immittance loop.

Now a new circle is calculated using the two 120-degree points(c) (triangles in Fig. 3) and the second intial point(i&c). Note that this new circle will be a better approximation to the immittance loop than was the previous one. This procedure iterates until two successive circles are within the desired tolerance. The result of this convergence is a "best-fit" circle, which is then divided into equal sectors, as shown in Fig. 4; the frequencies are found at each "triangle" location by applying Eq. (3).

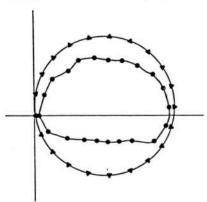


Fig. 4 - An immittance loop with a first-circle approximation.

Equally spaced points on the circle create quasi-equally spaced points on the immittance loop.

The HP 4192 Impedance Analyzer measures the conductance and susceptance at the "triangle" frequencies, and the immittance values are stored in a file. Note the dots on the immittance loop in Fig. 4 are not exactly "equally spaced", but certainly there is a better distribution of points(i)

than is obtained from a linear frequency sweep. This is what we previously referred to as quasi-equally spaced points(i).

#### CRITICAL FREQUENCIES

Once the loop is characterized with the desired number of quasiequally spaced points(i), specific frequency points(f) are needed for later calculations of various transducer parameters. The frequency points(f) [3] that are of interest are:

- f<sub>m</sub>: frequency at maximum admittance (minimum impedance)
- f<sub>n</sub>: frequency at maximum impedance (minimum admittance)
- fg: frequency at maximum conductance
- $\mathbf{f}_{\mathbf{p}}$ : frequency at maximum resistance
- f<sub>r</sub>: resonance frequency (susceptance is zero)
- fa: antiresonance frequency (susceptance is zero)
- $\mathbf{f_h}$ : frequency at maximum susceptance
- $\mathbf{f_1}$  : frequency at minimum susceptance
- f<sub>h</sub> : frequency at maximum reactance
- $\mathbf{f_1}$ : frequency at minimum reactance i

When characterizing an admittance loop, the frequency points(f)  $f_m$ ,  $f_s$ ,  $f_r$ ,  $f_p$ ,  $f_{h_a}$ , and  $f_{1_a}$  are determined by a maze technique that will be described in the program section of this report. When an impedance loop is characterized, the frequency points(f)  $f_a$ ,  $f_p$ ,  $f_n$ ,  $f_s$ ,  $f_h$ , and  $f_1$  are determined. One may note that the frequency sets differ when calculating

impedance or admittance loops. The authors believe that the two most important points(f) are the series and parallel resonance ( $f_g$  and  $f_p$ ). These points(f) can easily be found, and they occur for both loaded and unloaded transducers. Both of these conditions do not apply to the frequency pairs  $f_m$ ,  $f_n$  and  $f_a$ ,  $f_r$ . To determine the frequencies  $f_m$ ,  $f_n$  one must do a frequency sweep, which can be rather time consuming. The points(f)  $f_a$ ,  $f_r$  are easy to find by implementing root-finding techniques; however these points(f) do not always occur in loaded transducers. For these reasons, the focus has been on obtaining  $f_s$ ,  $f_p$ . The reader may note that  $f_g$  is the frequency at maximum conductance; however, it is not the frequency of minimum resistance as can be seen in Fig. 5.

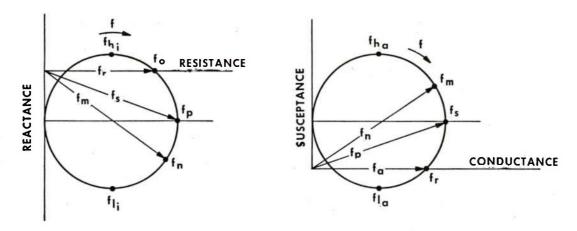


Fig. 5 - Impedance loop (5a) and admittance loop (5b), showing their critical frequencies.

Analogously,  $f_p$  is the frequency at maximum resistance; but it is not the frequency of minimum conductance.

The points(f) of secondary importance are the frequencies of minimum and maximum susceptance ( $f_{h_a}$  and  $f_{l_a}$ ). These points(f), sometimes called half-power points(f), are used to compute the electrical quality factor Q. We also compute the frequencies of minimum and maximum reactance ( $f_{h_r}$  and  $f_{l_r}$ ). These points(f), however, are not the half-power points(f) and cannot be used for calculating the quality factor Q. The only purpose for determining these points(f) is that they locate the frequencies at the top and bottom of the loop. The remaining frequencies are easily determined for the particular immittance loop calculated, and they serve as helpful

parameters for detecting problems.

## PROGRAM

The computer program MICAM, presented herein, is by no means the best implementation of the circular approximation method. However, the authors feel confident that this program can be refined in a manner that would be applicable in any research or manufacturing environment. The MICAM program, written in FORTRAN 77, is run on a Digital Equipment Corporation VAX 11/780 computer at the Underwater Sound Reference Detachment of the Naval Research Laboratory as a research tool as well as a quality-control problem detector. A version of this program is also written in HP Basic and can be executed on the HP 9836. The MICAM program has been tested on various transducers, both in air and in water, and seems to perform exceptionally well. It does have limitations, which will be explained in detail in the RESTRICTIONS section of this report. Since the program is quite involved, the line-by-line descriptions of MICAM and the program listings are included in Appendix B. The purpose of examining individual program lines is to:

- o Show how the algorithm has been implemented.
- o Give differences in admittance and impedance loops.
- Explain how critical frequencies are determined.

The program MICAM calls three subroutines; SIMEQ, RSORT, and FILE. The SIMEQ subroutine solves simultaneous equations. The RSORT subroutine sorts numbers in descending or ascending order. And the FILE subroutine stores the immittance information in FORTRAN files.

#### RESTRICTIONS

Limitations exist in all algorithms and should be used as one criteria for choosing one method over another. The following paragraphs identify two examples where a linear frequency sweep would be preferable to

determining frequencies by the circular approximation method.

One problem occurs when running very low-Q or highly damped transducers where no loops are formed. Since the circular approximation method is designed to emulate the immittance loop with a circle, the algorithm fails to converge on very low-Q or highly damped transducers. The MICAM program accommodates this problem by allowing the user to perform a frequency sweep. If the transducer is of low Q, a linear frequency sweep will give quasi-equally spaced points(i), as illustrated in Fig. 2.

A second problem occurs when two or more resonances are in the same frequency region. They may appear as small or large satellite loops.

Usually the small satellite loops are not a problem and MICAM will converge to the larger loop. Nevertheless, when immittance is the combination of loops of relatively the same size, MICAM converges to one of them, depending on the initial frequency given. This loop may not necessarily be the one desired. However, the authors feel that MICAM may be optimized for specific applications by relatively minor programming changes.

#### CONCLUSION

The circular approximation algorithm, when used with the HP 4192A Impedance Analyzer, makes a highly efficient system for measuring impedance and admittance of resonant electromechanical devices. The system has proven to be applicable to the measurement of active electromechanical materials as well as composite transducers. The algorithm has been used with excellent results on a VAX computer as well as on personal computers.

Although specifically developed as a research tool, the automated immittance measuring system is extremely well suited for quality-control and production testing of electromechanical transducers and materials.

#### **ACKNOWLEDGMENTS**

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#### APPENDIX A

#### Analysis for Applying Equations to Both Immittance Loops

The characteristic electrical property of a piezoelectric resonator is the equivalent series chain RLC in Fig. Al. The graphical representation of the RLC branch is more easily represented by the admittance which is represented as a circle referred to as the fiducial circle [1]. The graph can be easily extended to more complicated networks connected in parallel, such as  $C_{\rm O}$ .

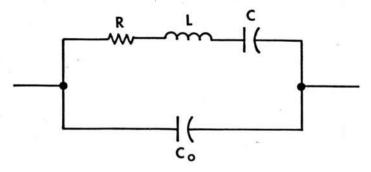


Fig. A1 - Simple equivalent circuit of a piezoelectric resonator.

The simple form of admittance of the RLC chain is all that is necessary to approximate the fiducial circle. The argument extends to the impedance representation in that all the information for the impedance circle is contained in the admittance circle. If

$$Y(\omega) = G(\omega) - jB(\omega),$$

then

$$\tan(\Theta) = \frac{-B(\omega)}{G(\omega)}.$$
 [A1]

Since  $Z(\omega)$  is the complex reciprocal of  $Y(\omega)$ ,  $Z(\omega)$  can be written as

$$Z(\omega) = \frac{G(\omega)}{G^2(\omega) + B^2(\omega)} + j \frac{B(\omega)}{G^2(\omega) + B^2(\omega)},$$
 [A2]

or Z(w) can be written as

$$Z(\omega) = R(\omega) + jX(\omega).$$
 [A3]

Equating the real and imaginary parts of Eqs. (A2) and (A3) results in the following expressions:

$$R(\omega) = \frac{G(\omega)}{G^2(\omega) + B^2(\omega)},$$
 [A4]

and

$$X(\omega) = \frac{B(\omega)}{G^2(\omega) + B^2(\omega)}.$$
 [A5]

For an impedance loop,  $tan(\theta)$  can be written as

$$\tan(\Theta) = \frac{X(\omega)}{R(\omega)},$$
 [A6]

or can be equivalently expressed by using Eqs. (A4) and (A5) as

$$\tan(\Theta) = \frac{-B(\omega)}{G(\omega)}.$$

Note that Eqs. (Al) and (A6) are identical except for being opposite in sign. Therefore for any  $\omega$  in the admittance circle there is a corresponding  $\omega$  of the same value in the impedance circle with the same but negative phase value.

#### APPENDIX B

#### Program Description and Listing

#### DESCRIPTION

This appendix contains a detailed description of MICAM as well as program listing. The program description supplements the CIRCULAR APPROXIMATION ALGORITHM section of this report and is necessary for a full understanding of this method. Program lines 1-76 are array declarations while lines 94-145 contain the interactive input section. There are several items of interest in this section. A question regarding speed is asked at line 98. Low speed provides an average measurement mode (approximately one measurement per second) to obtain measurement data of higher resolution and repeatability then at medium speed (5 measurements per second) or high speed (10 measurements per second). At line 112, the number of points(i) refers to the number of quasi-equally spaced points(i) that are desired on the immittance loop. In lines 118 and 120, the parallel or series resonance is required depending upon which loop is calculated. These frequencies are estimated from a priori knowledge. more confident one is of these points(f), the smaller the frequency step size can be taken (line 125).

Lines 138-163 is a section of code that allows the user to perform a frequency sweep. This is executed only if, for some reason, the circular approximation method does not apply. The portion of code that includes lines 176-215 is the location where the conductance and susceptance (resistance and reactance) for the three initial points(f) are determined. The ARRAY variable contains the coefficients of Eq. 4. In line 216, the subroutine SIMEQ solves the three simultaneous equations, which ultimately results in the center and radius of the circle given in lines 218-220.

The code from lines 221-237 is used to solve Eq. (2) for  $\omega_{\bf i}$  and 1/L, which are used to calculate the frequencies at two initial points(i) and the motional inductance value L (lines 241-250). Line 252 is a decision statement that determines if the difference between two successive series

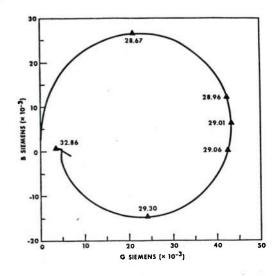
(parallel) resonant frequencies is within a desired tolerance. If the frequency is within tolerance, the program has determined the best fit  $\omega_1$  and L for Eq. (1). If the tolerance is not met, a new and hopefully better-fit circle will be computed using the frequencies at the two 120-degree points(c) (lines 261-283). These 120-degree frequency points(f) are found by solving Eq. (3) and substituting the recently computed values for  $\omega_1$  and L. This entire procedure repeats until the tolerance condition is met in line 252.

The second major computational portion of the MICAM program is found in lines 294-321. This portion uses the  $\omega_{i}$  and L that meet the tolerance specifications and Eq. (3) to calculate the quasi-equally spaced points(i). The remaining portion of the program determines the critical frequencies described earlier in this report. The RSORT subroutine sorts the data from the largest to the smallest value. In line 322, the conductance (resistance) is sorted so that the first value in the array will be the  $f_{s}$  ( $f_{p}$ ). The RSORT subroutine is called again in line 327 where frequency is the variable sorted. The remaining critical frequencies are determined by exercizing a maze technique. This technique is found in lines 337-384 and is based on previous knowledge on all immittance loops, shown in Fig. 5. The criteria used are:

$$f_m \le f_s \le f_r \le f_a \le f_p \le f_n.$$
 [B1]

A critical frequency point(f) is searched only in the region wherein it could occur; i.e, it satisfies the inequalities of Eq. (B1). All of the critical frequencies are chosen from the points(i&f) of the immittance loop except for  $f_p(f_g)$ . The points(f)  $f_p(f_g)$  require that more points(f) be calculated in order to have relatively accurate data. For example, when an admittance loop has been run,  $f_p$  is determined by switching the HP analyzer to the impedance mode, spotting the point(f)  $f_{1a}$ , and sweeping the frequency until the frequency at maximum impedance is found. On the other hand, when an impedance loop has been run, fs is determined by switching the analyzer to the admittance mode, spotting the point(f)  $f_{h_1}$ , and then sweeping the frequency in reverse until the frequency of maximum admittance is found. This technique is illustrated in lines 408-431.

The remaining portion of the program can be considered a formatted output section that prints a table of all critical frequencies described and files the data points(i) for plotting. The plots that can be created include a graph of magnitude of immittance verses frequency and a graph of the imaginary part of immittance verses the real part of immittance. Also the critical frequencies are stored so they may be overlayed on the immittance plot as shown in Figs. Bl and B2, which are examples of admittance loops obtained on a USRD Type F42A transducer in air and in the USRD Lake Facility by MICAM.



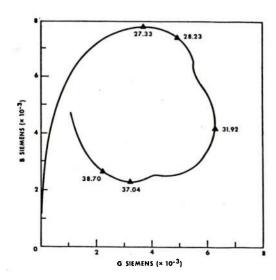


Fig. B1 - Admittance loop obtained on an F42A transducer in air.

Fig. B2 - Admittance loop obtained on an F42A transducer in the USRD Lake Facility.

There are several differences in MICAM for impedance or admittance loops. The first difference, of course, is that the HP analyzer is in the proper mode for the desired measurements (lines 171 and 172). Secondly, there is a difference in the motional resistance (R) found in Eqs.(1) through (3) for the two loops. In the admittance mode, R is approximated by the reciprocal of the diameter, and in the impedance mode, R is approximated by simply using the diameter of the circle. Two interactive runs of the program MICAM are included in Appendix B, which illustrate how

the user can obtain results in either immittance mode.

#### LISTING

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0001
0002
                MICAM PROGRAM
0003
        С
0004
0005
        С
                WRITTEN BY TINA RUGGIERO
0006
                FEBRUARY, 1983
        C
0007
0008 C THIS PROGRAM DETERMINES A FREQUENCY SWEEPING FUNCTION BY APPROXIMATING
0009
        C
                AN ADMITTANCE LOOP WITH A PERFECT CIRCLE. ALSO FN, FM,
0010
        С
                FA, FR, AND ADMITTANCE LOOPS ARE STORED AND ARE AVAILABLE
0011
        С
                FOR PLOTTING.
0012
0013
                DOUBLE PRECISION DEF(3), CONS(3), ARRAY(3,3), COEFF(3,3), COLUMN(3), ANS(3)
0014
                REAL RES(1000), XES(1000), FREQ(1000), X(6), Y(6), F(6), FR(3), FRE(1000)
0015
0016
                REAL K33, CE, CP, C0B, CAP, XCOF (5), COF (5), ROOTR (5), ROOTI (5), ADM (1000)
0017
                REAL CRX(8), CRY(9), MAG(1000)
                COMMON FR, AMR, RR, XR, FA, AMA, RA, XA, FM, AMM, RM, XM, FN, AMN, RN, XN, XH, XL
0018
0019
                COMMON RH, RL, FH, FL
                COMMON /LENGTH/LEN
0020
0021
0022
                BYTE ANSWER (80)
0023
0024
0025
                BYTE A(13)
                                                                            I VOLTS
0026
                DATA A /'O', 'L', 0, 0, 0, 0, 0, 0, 0, 0, 0, 'E', 'N'/
0027
                BYTE B(12)
0028
                                                                            ! START
0029
                DATA B /'T', 'F', 0, 0, 0, 0, 0, 0, 0, 0, 0, 'E', 'N'/
0030
                BYTE C(13)
                                                                             I STOP
0031
0032
                DATA C /'P', 'F', 0, 0, 0, 0, 0, 0, 0, 0, 0, 'E', 'N'/
0033
                BYTE D(12)
                                                                             I STEP
0034
                DATA D /'S', 'F', 0, 0, 0, 0, 0, 0, 0, 0, 'E', 'N'/
0035
0036
                                                                             I SPOT
0037
                BYTE E(13)
0038
                DATA E /'F', 'R', 0, 0, 0, 0, 0, 0, 0, 0, 0, 'E', 'N'/
0039
                BYTE IDSP(4)
0040
                DATA IDSP /'F', '1', 'A', '4'/
                                                           IDISPLAY CAP
                                                                           DIS
0041
                BYTE IADV(2)
                                                                           ISTEP UP
0042
0043
                DATA IADV /'W', '2'/
0044
                                                                         ISTEP DOWN
0045
                BYTE IREV(2)
                DATA IREV /'W', '4'/
0046
0047
0048
                BYTE IAD1(2)
0049
                DATA IAD1 /'D', '1'/
                                                                  IDATA READY ON
0050
0051
                BYTE IADO(2)
```

0052		DATA IADO /'D', '0'/	IDATA READY OFF
0053			
0054		BYTE IADM(4)	
0055		DATA IADM/'F', '1', 'A', '2'/	IDISPLAY G
0056			_
0057		BYTE IAV1(2)	AVERAGE ON
0058		DATA IAV1/'V', '1'/	
0059			
0060		BYTE IAH1(2)	IHIGH SPEED ON
0061		DATA IAH1/'H', '1'/	
0062			
0063		BYTE IAHO(2)	IHIGH SPEED OFF
0064		DATA IAHO/'H', 'O'/	
0065			
0066		BYTE IAMM(2)	IMANUAL SWEEP
0067		DATA IAMM/'W', '0'/	
0068			
0069		BYTE IAC3(2) IP	ARALLEL CIRCUIT (ADMITTANCE)
0070		DATA IAC3/'C', '3'/	
0071			
0072		BYTE IAC2(2)	SERIES CIRCUIT (IMPEDANCE)
0073		DATA IAC2/'C', '2'/	
0074			
0075		BYTE IAEX(2)	ITRIGGER THE READING
0076		DATA IAEX/'E', 'X'/	
0077			
0078		IADDR=1	
0079		ITIMO=30	
0080		LUN=1	
0081		CALL BTAKEC (LUN, ISTAT)	ITAKE CHARGE OF GPIB
0082		CALL BDEVCL(IADDR, ISTAT)	ICLEAR SELECTED DEVICE
0083			
0084		CALL ERRSET(64,,.FALSE.,,.FALSE	.,,) IIGNORE ERROR MESSAGE 64
0085			
0086		CALL BWRITE (IADDR, IADM, 4, ISTAT)	IDISPLAY MODE
0087			
0088		AMM=10000.	
0089		LENGTH1=35	
0090		LENGTH2=21	
0091		LENGTH3=80	
0092	1053	FORMAT(F9.5)	
0093		AMN=0.	
0094		WRITE (5, 888)	
0095	888	FORMAT('\$DO YOU WANT 1)IMPEDANO	CE 2) ADMITTANCE ')
0096		READ (5, 889) ILOOP	
0097	889	FORMAT(I2)	
0098		WRITE (5, 900)	
0099	900	FORMAT("\$", "DO YOU WANT 1) LOW, 2	) MED. 3) HIGH SPEED ')
0100		READ (5, 950) IAVE	
0101	950	FORMAT(I2)	
0102	7 -		

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0103
               WRITE (5, 1000)
        10
               FORMAT(/'$', 'ENTER THE VOLTAGE LEVEL (IN VOLTS):
                                                                         •)
        1000
0104
0105
               READ (5, 1060, ERR=10) VOLTS
0106
               ENCODE (9, 1070, A(3)) VOLTS
               CALL BWRITE (IADDR, A, 13, ISTAT)
0107
0108
        1060
               FORMAT(F10.0)
        1070
0109
               FORMAT(F9.4)
               NTIMES=1
0110
0111
0112
               WRITE(5, 1111)
               FORMAT( '$ ENTER # OF POINTS ')
0113
        1111
0114
               READ (5, 1020) NPTS
        1020
0115
               FORMAT(I4)
        20
                 NTIMES=NTIMES+1
0116
0117
               IF (ILOOP .EQ. 1) WRITE (5, 1010)
0118
        1010
                   FORMAT(/'$', 'ENTER FREQUENCY(PARALLEL RESONANCE) (IN KHZ):
0119
0120
               IF (ILOOP .EQ. 2) WRITE (5, 1011)
        1011
                   FORMAT(/'$', 'ENTER FREQUENCY(SERIES RESONANCE) (IN KHZ):
0121
               READ (5, 1060, ERR=20) START_FREQ
0122
               ITIME=1
0123
0124
0125
               WRITE (5, 1030)
        1030
                   FORMAT ('SENTER STEP FREQ (IN KHZ):
0126
               READ(5, 1060)STEP_FREQ
0127
0128
               IF (NTIMES .LT. 5) THEN
                   GOTO 3000
0129
0130
               ELSE
0131
                 TYPE *, 'DO YOU WANT TO SWEEP FREQ?'
                 READ(5, 1035) ISWEEP
0132
0133
        1035
                     FORMAT(A2)
                 IF (ISWEEP . EQ. 'N') THEN
0134
0135
                   NTIMES=-10
0136
                   GO TO 3000
0137
                 END IF
               1=1
0138
0139
               ENCODE (8, 1066, D(3)) STEP_FREQ
0140
               CALL BWRITE (IADDR, D, 12, ISTAT)
               WRITE (5, 1040)
0141
0142
        1040
                   FORMAT(/, 'SENTER THE STOPPING FREQ (KHZ) ')
               READ (5, 1060) STOP
0143
               ENCODE (9, 1070, C(3)) STOP
0144
0145
        1066
                   FORMAT(F8.4)
               CALL BWRITE (IADDR, C, 13, ISTAT)
0146
                                                                    ISPOT FREQUENCY
0147
               ENCODE (9, 1070, E(3)) START_FREQ
0148
               CALL BWRITE (IADDR, E, 13, ISTAT)
0149
0150
               CALL BWRITE (IADDR, IAMM, 2, ISTAT)
                                                                      !MANUAL MODE
0151
        1044
                   CALL BWRITE (IADDR, IAEX, 2, ISTAT)
                                                                         !TRIGGER
               DO J=1,80
0152
                 ANSWER(J)=0
0153
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0154
               END DO
0155
               CALL BREAD (IADDR, ANSWER, LENGTH3, ISTAT)
0156
               DECODE (12, 1050, ANSWER (5)) RES (I)
0157
               DECODE (12, 1050, ANSWER (21)) XES (I)
0158
               DECODE (9, 1053, ANSWER (35)) FREQ (I)
0159
               IF (FREQ(I) .GE. STOP)GOTO 88
0160
               CALL BWRITE (IADDR, IADV, 2, ISTAT)
                                                                    IADVANCE FREQ.
0161
               |≈|+1
0162
               GO TO 1044
               END IF
0163
        3000
0164
                    STEPI=STEP_FREQ
0165
               IF (IAVE.EQ.1) CALL BWRITE (IADDR, IAV1, 2, ISTAT)
                                                                    IAVERAGE SPEED
0166
0167
               IF (IAVE .EQ. 3) CALL BWRITE (IADDR, IAH1, 2, ISTAT)
                                                                        IHIGH SPEED
0168
               IF (IAVE .EQ. 2) CALL BWRITE (IADDR, IAHO, 2, ISTAT)
                                                                      INORMAL SPEED
0169
0170
               CALL BWRITE (IADDR, IAMM, 2, ISTAT)
                                                                       IMANUAL MODE
0171
               IF (ILOOP .EQ. 2) CALL BWRITE (IADDR, IAC3, 2, ISTAT) ICIRCUIT TYPE 3
0172
               IF (ILOOP . EQ. 1) CALL BWRITE (IADDR, IAC2, 2, ISTAT) !CIRCUIT TYPE 2
0173
0174
        48
                  IF (IT .GT. 1) CONTINUE
0175
                  DO I=1,3
0176
        49
0177
                  IF (ITIME .GE. 2) THEN
0178
                       IF (I .EQ. 2) GOTO 85
0179
                       FREQUENCY=ABS (FR(I)/(1000.*2*3.14159))
0180
                        ENCODE (9, 1070, E(3)) FREQUENCY
                                                              I SPOT STARTING POINT
0181
                        CALL BWRITE (IADDR. E. 13, ISTAT)
0182
                         FREQ(I)=FREQUENCY
0183
                   ELSE
0184
                        ENCODE (9, 1070, E(3)) START_FREQ
                                                              I SPOT STARTING POINT
                        CALL BWRITE (IADDR, E, 13, ISTAT)
0185
0186
                       FREQ(I)=START_FREQ
                  END IF
0187
0188
                  CALL BWRITE (IADDR, IAEX, 2, ISTAT)
                                                            ITRIGGER THE READING
0189
                  DO J=1,80
0190
0191
                    ANSWER (J)=0
0192
                   END DO
                   K=0
0193
0194
                  CALL BREAD (IADDR, ANSWER, LENGTH1, ISTAT)
0195
                  DECODE (12, 1050, ANSWER (5)) RES (1)
0196
                  DECODE (12, 1050, ANSWER (21) )XES (1)
0197
        1050
                      FORMAT (E12.2)
0198
                  IF (ITIME, EQ. 1, AND, I, EQ. 1) THEN
                     FREQA=FREQ(1)
0199
0200
                     XESA=XES(1)
                     RESA=RES(1)
0201
                  ELSE
0202
0203
                  END IF
                  FREQ(I)=FREQ(I)*1000
0204
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0205
       85
                  ARRAY(I, 1)=RES(I)
0206
                ARRAY (1, 2) = XES (1)
0207
                ARRAY (1, 3)=1.
0208
                CONS(I) = -(RES(I)*RES(I)*XES(I)*XES(I))
0209
                IF (ITIME.EQ. 1) START_FREQ=START_FREQ+STEP_FREQ
0210
              END DO
0211
0212
       С
                SIMEQ IS A SUBROUTINE THAT SOLVES SIMELTANEOUS EQUATIONS
0213
                 USED TO FIND COEFICIENTS OF A GENERALIZED CIRCLE
0214
0215
              N=3
                                                         INUMBER OF PARAMETERS
0216
              CALL SIMEQ(N, ARRAY, CONS, DEF)
              IF(N .EQ. 0)GO TO 20
0217
0218
              CENTERX=-DEF(1)/2.
                                                              IX VALUE OF CENTER
0219
              CENTERY=-DEF(2)/2.
                                                              IY VALUE OF CENTER
              RADIUS=.5*SQRT(DEF(1)*DEF(1)+DEF(2)*DEF(2)-4*DEF(3))
0220
0221
              IF (ILOOP .EQ. 2) RESIS=1./(2*RADIUS)
                                                       !RESISTANCE (ADMITTANCE)
0222
              IF (ILOOP . EQ. 1) RESIS=2*RADIUS
                                                        !RESISTANCE (IMPEDANCE)
0223
0224
       С
               SLOPE IS THE TAN (THETA) IN EQUATION 1
0225
0226
              SLOPE1=((XES(1)-CENTERY)/(RES(1)-CENTERX+RADIUS))
              SLOPE2=((XES(2)-CENTERY)/(RES(2)-CENTERX+RADIUS))
0227
0228
              SLOPE3=((XES(3)-CENTERY)/(RES(3)-CENTERX+RADIUS))
0229
0230
              COEFF (1, 1)=SLOPE1*RESIS*6.283185*FREQ(1)
0231
              COEFF (2, 1)=SLOPE2*RESIS*6.283185*FREQ(2)
0232
              COEFF (1, 2)=1.
0233
              COEFF(2,2)=1.
0234
              COLUMN(1)=(2*3.14159*FREQ(1))**2
              COLUMN (2) = (2*3, 14159*FREQ(2)) **2
0235
0236
0237
0238
              CALL SIMEQ (N, COEFF, COLUMN, ANS)
0239
              IF(N .EQ. 0)GOTO 20
0240
                ANS(1) is the Inductor
0241
       C
0242
                ANS(2) is the Resonant Freq.
0243
              IF (ANS (2) .LT. 0) GOTO 20
0244
0245
              ANS(1)=1/ANS(1)
              ANS(2)=SQRT(ANS(2))
0246
0247
              IF(ANS(2) .EQ. 0)GOTO 20
0248
              RESONANCE=ANS (2) /6283, 185
              WRITE (5, 77) ANS (2) /6283.185
0249
                FORMAT(' FREQ= ',F10.3)
0250
       77
0251
0252
              IF(ABS(ANS(2)-OMEGA)/6283.LE.(.0005*FREQA) .OR. ITIME .GE. 25)THEN
0253
                  ANS(2)=(OMEGA+ANS(2))/2.
0254
                 ANS(1)=(RINDUCTOR+ANS(1))/2.
0255
                 GOTO 50
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```
0256
              ELSE
0257
                OMEGA=ANS(2)
0258
                RINDUCTOR=ANS(1)
0259
              END IF
0260
               ANGLES OF OTHER 2 POINTS
0261
       C
0262
0263
              TRANSX1=RES(2)-CENTERX
0264
              TRANSY1=XES(2)-CENTERY
              TRANSA1=ATAN2(TRANSY1, TRANSX1)
0265
              X2=COS (TRANSA1+2.094395) *RADIUS+CENTERX
0266
0267
              X3=COS (TRANSA1-2,094395) *RADIUS+CENTERX
0268
              Y2=SIN (TRANSA1+2, 094395) *RADIUS+CENTERY
0269
              Y3=SIN (TRANSA1-2, 094395) *RADIUS+CENTERY
0270
0271
              SLOPE1= (Y2-CENTERY) / (X2-CENTERX+RADIUS)
0272
              SLOPE3= (Y3-CENTERY) / (X3-CENTERX+RADIUS)
0273
              B1=-SLOPE1*RESIS
0274
              B2=-SLOPE2*RESIS
0275
              B3=-SLOPE3*RESIS
0276
0277
              FR(1)=-B1-SQRT(B1*B1+4.*ANS(1)**2*(ANS(2)*ANS(2)))
0278
              FR(1)=FR(1)/(2*ANS(1))
0279
              FR(2)=FREQ(2)*2*3.14159
0280
              FR(3)=-B3-SQRT(B3*B3+4.*ANS(1)**2*(ANS(2)*ANS(2)))
0281
              FR(3)=FR(3)/(2*ANS(1))
0282
              ITIME=ITIME+1
0283
              IF (ITIME .GE. 2) GOTO 49
0284
       50
                R=SQRT(RESA*RESA+XESA*XESA)
0285
              THETA=ATAN2 (XESA, RESA)
              A0=SQRT ((CENTERX-RESA) **2 + (CENTERY-XESA) **2)
0286
0287
              CONVERT=1,74532E-02
0288
              TIM=359./NPTS
0289
              PI=3,14159
0290
              TRANSX=RESA-CENTERX
              TRANSY=XESA-CENTERY
0291
0292
              THETA=ATAN2 (TRANSY, TRANSX)
0293
              1=1
0294
              DO IT=1, NPTS
0295
              DELTA2=IT*TIM*CONVERT+THETA
0296
              X3=(COS(DELTA2)*RADIUS)+CENTERX
              Y3= (SIN (DELTA2) *RADIUS) +CENTERY
0297
0298
                SLOPE3= (Y3-CENTERY) / (X3-CENTERX+RADIUS)
0299
                B3=-SLOPE3*RESIS
0300
0301
0302
                FRE(I)=-B3+SQRT(B3*B3+4, *ANS(1)**2*(ANS(2)*ANS(2)))
0303
                FRE(I)=FRE(I)/(2.*ANS(1))
0304
                FREQUENCY=ABS(FRE(I)/(1000.*2*3.14159))
                 TOLERANCE1=2.5*RESONANCE
0305
       9
0306
                IF (FREQUENCY .GT. TOLERANCE1)GOTO 70
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0307
                        ENCODE (9, 1070, E(3)) FREQUENCY | SPOT STARTING POINT
0308
                  CALL BWRITE (IADDR, E, 13, ISTAT)
                  CALL BWRITE (IADDR, IAEX, 2, ISTAT)
                                                          ITRIGGER THE READING
0308
0310
                 DO J=1,80
0311
                     ANSWER (J)=0
                  END DO
0312
0313
                  K=0
0314
                 CALL BREAD (IADDR, ANSWER, LENGTH1, ISTAT)
0315
                 DECODE (12, 1050, ANSWER (5)) RES (1)
0316
                 DECODE (12, 1050, ANSWER (21)) XES (I)
0317
                 IF(RES(I) .GT. 1.3E6 .OR. XES(IT) .GT. 1.3E6)GO TO 70
0318
                 FREQ(I)=FREQUENCY
                  MAG(I)=SQRT(RES(I)*RES(I)+XES(I)*XES(I))
0319
0320
                 I=I+1
0321
        70
                 END DO
                 CALL RSORT (RES, FREQ, XES, I-1, 1)
0322
0323
               GS=RES(1)
0324
               BS=XES(1)
0325
               FS=FREQ(1)
0326
               TANO=ATAN2(BS, GS)
0327
               CALL RSORT(FREQ, RES, XES, I-1, 1)
               FLAG=0
0328
               IT=2
0329
               XESMAX=-1E12
0330
0331
               RESMAX=-1E12
0332
               XESMIN=1E12
0333
               RESMIN=1E12
0334
               ADMMIN=1E12
0335
               ADMMAX=0
               TANMIN=1E12
0336
0337
               DO J=2, I-1
                 IF(XES(J) .GT. BS .AND. FLAG .EQ.O .AND. XES(J) .GT. 0)THEN
0338
                    FREQ(1)=FREQ(J)
0339
0340
                    RES(1)=RES(J)
                    XES(1)=XES(J)
0341
                    GO TO 500
0342
0343
                 ELSE
0344
                    FREQ(IT)=FREQ(J)
0345
                    RES(IT)=RES(J)
0346
                    XES(IT)=XES(J)
0347
                    TAN1=ATAN2(XES(IT), RES(IT))
0348
                    FLAG=1
0349
                     ADM(IT)=SQRT(RES(IT)**2 +XES(IT)**2)
0350
                    IF(FREQ(IT) .LE. FS .AND. IT .GT. 1)THEN
0351
                      IF (XES(IT) .GE. XESMAX) THEN
0352
                         XESMAX=XES(IT)
0353
                        FH=FREQ(IT)
0354
                        GH=RES(IT)
0355
                        BH=XES(IT)
0356
                      END IF
0357
                      IF (ADM (IT) . GT. ADMMAX . AND. ILOOP . EQ. 2) THEN
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```
0358
                         ADMMAX=ADM (IT)
0359
                         FM=FREQ(IT)
0360
                         GM=RES(IT)
0361
                         BM=XES(IT)
0362
                      END IF
0363
                      IF (XES (IT-1) .LT. 0 .AND. XES (IT) .GT. 0) THEN
0364
                         FRES=FREQ(IT)
0365
                         GR=RES(IT)
0366
                         BR=XES(IT)
0367
                       END IF
0368
                    END IF
                     IF (FREQ (IT) .GE. FS .AND. IT .GT. 1) THEN
0369
                      IF (XES (IT) .LE. XESMIN) THEN
0370
0371
                         XESMIN=XES(IT)
0372
                         FL=FREQ(IT)
0373
                         GL=RES(IT)
0374
                         BL=XES(IT)
0375
                       END IF
0376
                        IF (XES(IT-1) .LT. 0 .AND. XES(IT) .GT. 0) THEN
0377
                         FRES=FREQ(IT)
0378
                       GR=RES(IT)
0379
                         BR=XES(IT)
0380
                       END IF
0381
                        IF (ADM (IT) , GT, ADMMAX .AND. ILOOP .EQ. 1) THEN
0382
                          ADMMAX=ADM(IT)
                          FN=FREQ(IT)
0383
0384
                                GN=RES(IT)
0385
                         BN=XES(IT)
0386
                        ENDIF
0387
                     END IF
                  IT=IT+1
0388
                  END IF
0389
0390
        500
                   END DO
0391
                IF (ILOOP, EQ. 1) THEN
0392
                WRITE (5, 1109)
        1109
                    FORMAT (///, 9X, 'TYPE', 11X, 'FREQUENCY (KHZ)', 2X, 'RESISTANCE', 2X,
0393
0394
                1'REACTANCE')
                ELSE
0395
0396
                WRITE (5, 1110)
                    FORMAT(///, 9X, 'TYPE', 11X, 'FREQUENCY (KHZ)', 2X, 'CONDUCTANCE', 2X,
0397
        1110
0398
                1'SUSCEPTANCE')
0399
                END IF
0400
                WRITE (5, 1112)
0401
        1112
                    FORMAT (9X, '----', 11X, '-
                                                        --', 2X, '--
                12X,'----',/)
0402
0403
                IF (FRES . EQ. 0) THEN
                  IF (BL .LT. 0) THEN
0404
0405
                     FRES=FS
0406
                     GR=GS
0407
                     BR=BS
0408
                     WRITE (5, 1130) FRES, GR, BR
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```
0409
                  ELSE
0410
                   WRITE (5, 1120)
                      FORMAT (1X, 'RESONANCE', 17X,' DOES NOT EXIST')
0411
        1120
                 END IF
0412
0413
               ELSE
0414
                  IF (ILOOP .EQ. 2) WRITE (5, 1130) FRES, GR, BR
                      FORMAT (1X, 'RESONANCE', 16X, F8.3, 7X, E8.3, 5X, E9.3)
0415
        1130
0416
                  IF (ILOOP . EQ. 1) WRITE (5, 1131) FRES, GR, BR
0417
        1131
                      FORMAT (1X, 'ANTIRESONANCE', 12X, F8.3, 7X, E8.3, 5X, E9.3)
               END IF
0418
0419
               CALL BWRITE (IADDR, IAMM, 2, ISTAT)
                                                                       !MANUAL MODE
               FLAG1=0
0420
                                                                         ISTEP SIZE
               ENCODE (8, 1066, D(3)).1
0421
               CALL BWRITE (IADDR, D, 12, ISTAT)
0422
               IF (ILOOP .EQ. 1) CALL BWRITE (IADDR, IAC3, 2, ISTAT)
0423
0424
               IF (ILOOP .EQ. 2) CALL BWRITE (IADDR, IAC2, 2, ISTAT)
                IF(ILOOP .EQ. 2)ENCODE(9, 1070, E(3))FL
0425
               IF (ILOOP .EQ. 1) ENCODE (9, 1070, E(3)) FH
0426
                                                                              ISPOT
0427
               CALL BWRITE (IADDR, E, 13, ISTAT)
0428
                GP=0
0429
        1270
                    CALL BWRITE (IADDR, IAEX, 2, ISTAT)
               DO J=1,80
0430
                 ANSWER(J)=0
0431
0432
                END DO
0433
                CALL BREAD (IADDR, ANSWER, LENGTH3, ISTAT)
0434
                DECODE (12, 1050, ANSWER (5)) A1
0435
                DECODE (12, 1050, ANSWER (21)) B1
                DECODE (9, 1053, ANSWER (35)) F1
0436
0437
                IF (A1 .GE. GP )THEN
0438
                  FP=F1
0439
                  GP=A1
                  BP=B1
0440
                  IF (ILOOP .EQ. 2) CALL BWRITE (IADDR, IADV, 2, ISTAT)
                                                                            !ADVANCE
0441
                                                                            !REVERSE
0442
                   IF (ILOOP .EQ. 1) CALL BWRITE (IADDR, IREV, 2, ISTAT)
                  GO TO 1270
0443
                ELSE
0444
                  FLAG1=FLAG1+1
0445
                  IF (FLAG1 . EQ. 1) THEN
0446
                     IF (ILOOP.EQ.2) CALL BWRITE (IADDR, IADV, 2, ISTAT)
0447
                     IF (ILOOP, EQ. 1) CALL BWRITE (IADDR, IREV, 2, ISTAT)
0448
                     FP=F1
0449
0450
                    GP=A1
                    BP=B1
0451
                    GOTO 1270
0452
0453
                  END IF
0454
                END IF
                NUM=8
0455
                CRX(1)=GS
0456
                CRY(1)=BS
0457
0458
                CRX(2)=GP
0459
                CRY(2)=BP
```

```
0460
                CRX (3) = GM
0461
                CRY(3)=BM
0462
                CRX(4)=GN
0463
                CRY(4)=BN
0464
                CRX(5)=GH
0465
                CRY(5)=BH
0466
                CRX(6)=GL
0467
                CRY(6)=BL
0468
                IF (FRES .EQ. 0) THEN
0469
                  NUM=NUM-1
0470
                ELSE
0471
                  CRX(7)=GR
0472
                  CRY(7)=BR
                END IF
0473
0474
                IF (FA .EQ. 0) THEN
0475
                  NUM=NUM-1
0476
                ELSE
0477
                  CRX(8)=GA
                  CRY(8)=BA
0478
                END IF
0479
0480
                  IF (ILOOP .EQ. 2) WRITE (5, 1160) FS, GS, BS
0481
                  IF (ILOOP .EQ. 1) WRITE (5, 1160) FP, GP, BP
        1160
                      FORMAT (1X, 'SERIES RESONANCE', 9X, F8.3, 7X, E8.3, 5X, E9.3)
0482
0483
                  IF (ILOOP .EQ. 2) WRITE (5, 1170) FP, GP, BP
0484
                  IF (ILOOP .EQ. 1) WRITE (5, 1170) FS, GS, BS
        1170
                      FORMAT (1X, 'PARALLEL RESONANCE', 7X, F8.3, 7X, E8.3, 5X, E9.3)
0485
0486
                  IF (ILOOP .EQ. 2) WRITE (5, 1180) FM, GM, BM
0487
        1180
                      FORMAT (1X, 'MAXIMUM ADMITTANCE', 7X, F8.3, 7X, E8.3, 5X, E9.3)
0488
                   IF (ILOOP . EQ. 1) WRITE (5, 1280) FN, GN, BN
0489
        1280
                      FORMAT (1X, 'MAXIMUM IMPEDANCE', 8X, F8.3, 7X, E8.3, 5X, E9.3)
0490
                   WRITE (5, 1190) FH, GH, BH
0491
        1190
                      FORMAT (1X, 'HIGH POINT', 15X, F8.3, 7X, E8.3, 5X, E9.3)
0492
                  WRITE (5, 1200) FL, GL, BL
                      FORMAT(1X, 'LOW POINT', 16X, F8.3, 7X, E8.3, 5X, E9.3)
        1200
0493
0494
                WRITE (5, 1300) 7
0495
        1300
                    FORMAT(//, ' ', A1)
                 IF(ILOOP .EQ. 2) TYPE *, 'ADMITTANCE LOOP'
0496
                IF (ILOOP . EQ. 1) TYPE *, 'IMPEDANCE LOOP'
0497
0498
                CALL FILE (IT-1, RES, XES)
0499
                TYPE *,' '
0500
                TYPE *, 'CRITICAL FREQUENCIES'
                CALL FILE (NUM, CRX, CRY)
0501
0502
                TYPE *,' '
0503
                TYPE *, 'FREQ VS. MAG.'
0504
                CALL FILE (IT-1, FREQ, MAG)
                CALL BDEVCL (IADDR, ISTAT)
                                                                     ICLEAR SELECTED
0505
0506
                END
```

## APPENDIX C

#### Running MICAM

RUN SUPER

DO YOU WANT 1) IMPEDANCE 2) ADMITTANCE 1

DO YOU WANT 1) LOW, 2) MED, 3) HIGH SPEED 3

ENTER THE VOLTAGE LEVEL (IN VOLTS): .1
ENTER # OF POINTS 100

ENTER FREQUENCY (PARALLEL RESONANCE) (IN KHZ): 15

ENTER STEP FREQ (IN KHZ): .5

FREQ= 15.304

FREQ= 15.293

FREQ= 15.291

TYPE	FREQUENCY(KHZ)	RESISTANCE	REACTANCE
ANTIRESONANCE	15.291	.107E+07	0.100E+05
SERIES RESONANCE	14.384	.485E-02	288E-02
PARALLEL RESONANCE	15.291	.107E+07	0.100E+05
MAXIMUM IMPEDANCE	15.291	.107E+07	0.100E+05
HIGH POINT	15.284	.530E+06	0.530E+06
LOW POINT	15.297	.630E+06	540E+06

IMPEDANCE LOOP

FILE NAME FOR X,Y DATA: DATA1

CRITICAL FREQUENCIES

FILE NAME FOR X,Y DATA: DATA2

FREQ VS. MAG.

FILE NAME FOR X,Y DATA: DATA3

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RUN SUPER

DO YOU WANT 1) IMPEDANCE 2) ADMITTANCE 2

DO YOU WANT 1) LOW, 2) MED, 3) HIGH SPEED 3

ENTER THE VOLTAGE LEVEL (IN VOLTS): .1

ENTER # OF POINTS 100

ENTER FREQUENCY(SERIES RESONANCE) (IN KZH): 14

ENTER STEP FREQ (IN KHZ): .5

FREQ= 14.390

FREQ= 14.372

FREQ= 14.372

TYPE	FREQUENCY(KHZ)	CONDUCTANCE	SUSCEPTANCE
RESONANCE	14.375	.678E-02	0.300E-04
SERIES RESONANCE	14.373	.679E-02	0.540E-03
PARALLEL RESONANCE	15.291	.107E+07	0.000E+00
MAXIMUM ADMITTANCE	14.373	.677E-02	0.790E-03
HIGH POINT	14.357	.311E-02	0.379E-02
LOW POINT	14.391	.327E-02	316E-02

ADMITTANCE LOOP

FILE NAME FOR X,Y DATA: DATAL

CRITICAL FREQUENCIES

FILE NAME FOR X,Y DATA: DATA2

FREQ VS. MAG.

FILE NAME FOR X,Y DATA: DATA3

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